**Introduction.** Structural damage identification is a fundamental element following an earthquake. A correct definition of the damage state of buildings allows us to establish technical procedures and operational standards for safeguarding the structures, aimed at restoring their original conditions.

Structural Health Monitoring techniques (SHM) make it possible to deduce the presence of lesions and estimate the severity of the damage to the structures by measuring the mode of vibration of the buildings. This is possible because the dynamic response of structures is strongly influenced by the conservation state of materials and by structural lesions. The scientific literature includes many methods of structural dynamic response evaluation and algorithms for the extraction of main modal parameters (Ivanovic et al., 2000; Sohn et al., 2004). Several experimental configurations are classified in function of the number of measured output signals (number of sensors) and of the type of sources used to energize the structures. In this context there are several experimental layouts to modal parameters identification. Specifically, it is possible to differentiate in forced vibration tests (i.e. using mechanical shaker or vibrodines), free vibration tests (i.e. by means of falling objects inside or outside the buildings – impulsive signals) and ambient vibration tests (i.e. using random sources as wind and artificial noise) (Maia et al., 1997). The last methods are very useful for assessing dynamic behaviour and for a rapid evaluation of the true conditions of existing damaged structures after an earthquake. However, the most common data acquisition techniques use in-contact sensors. Velocimeters or accelerometers arrays are placed inside the building and are used to record time series of ambient vibration. In the last decade, advances in the field of Ground Based Remote Sensing assure remote data acquisition and real-time monitoring of vibrations in critical conditions, as well as dynamic control of severely damaged structures after earthquakes. In this paper the authors propose a procedure for assessing the state of damage to structures in areas affected by earthquakes. This approach is founded on remote monitoring techniques of mechanical vibrations by means of interferometric surveys. This method allows us to ensure maximum safety conditions during the monitoring of potentially damaged structures. In fact, the assessment of the structural damages during the next phase is extremely delicate due to precarious stability conditions of structures and due to possible further aftershocks during technical inspections by specialists. For this reason a new application of this proposed operational approach will be discussed in the case of the Emilia earthquake (Italy) for the stability control of the bell tower of San Giacomo Roncole using IBIS-S ground-based microwave interferometer.

**Instrumental features of the IBIS-S technology.** Microwave interferometry has recently emerged as a new technology, specifically suitable to remotely measuring the vibration response of structures. Several authors observe that the interferometric technique has proven to be a useful remote sensing tool for vibration measurements of structures, such as architectural heritage structures (Pieraccini et al., 2005, 2009; Atzeni et al., 2010), engineering infrastructures (Gentile and Bernardini, 2008 and 2009) and vibrating stay cables (Gentile, 2010 a, b). This radar technology is founded on the combined use of high-resolution waveforms (Wehner, 1995) and interferometric technique (Henderson, 1998). This technique is implemented to compute the displacement of each target through the phase shift \( \Delta \phi \) of the back-scattered microwave signals collected at different time intervals. The displacement along the radar line of sight \( d \) is computed from the phase-shift with the following simple Eq. (1):
where $\lambda$ is the wavelength of the signal (Taylor, 2001). The main advantages of the interferometric radar for structural health monitoring of civil infrastructures are high accuracy of measurements (sensitivity of 0.01-0.02 mm) and high spatial resolution, simultaneous monitoring of several targets within the sensor applicable distance, independence from daylight and weather conditions for short recordings, portability, and quick set-up time. The sensor module is provided with two horn antennas (-3dB beamwidth of 17° and 15° in the horizontal and vertical plane) and transmits the electromagnetic signals in Ku frequency band from 17.1 to 17.3 GHz, receiving the echoes from several targets placed inside the radar scenario.

The acquired time history $s(t)$ is the displacement of the target projected along the sensor-target line of sight (LOS). The LOS displacement $s(t)$ is linked to the displacements component $V(t)$ and $H(t)$, in vertical and in horizontal plane respectively, through the following Eq. (2):

$$s(t) = V(t)\sin(\beta) + H(t)\cos(\beta)$$

with $\beta$ being the LOS angle computed from the horizontal axis. The interferometric survey may thus be considered a powerful tool to evaluate the deformation related to dynamic applied loads and to evaluate the stiffness of structures.

**Description and method.** The test site was chosen in order to analyze a strongly damaged but not totally crushed bell tower, for which remote sensing approach was the only compatible one with safety conditions. The experimental settings were designed with the task to have comparable results from two main acquisition distances from the target and two different direction projection of measured displacement.

The bell tower: a brief historical overview and description of the damage. The Emilia earthquake has caused numerous damages to the structures. The buildings most affected by the earthquake are industrial structures (factories and storage magazines) and cultural heritage buildings (churches, bell towers, civic towers, etc.), whose geometric and constructive features have contributed to increasing their vulnerability in case of earthquakes. In this work we present the study performed for the bell tower of San Giacomo Roncole. The actual structure was built from 1771 to 1774 with the same materials of the previous Carmelite Convent of Santa Maria delle Grazie della Galeazza (Andreoli, 1987). The building is located few metres away from the singular nave of the church. The structure replaced an earlier tower, adjacent to the body of the church and demolished by the damage caused by the vibrations of the bells. The new tower is a masonry structure located at South-west of the church. The tower reaches a height of about 36 metres with a square base (5 metres per side). After the earthquakes of 20th and 29th May 2012 (magnitude $M_L=5.9$ and $M_L=5.8$, respectively) the building sustained serious damage to the base, highlighted by displacements of about 2 cm toward the South-West side and of 1 cm on the South-East side. In other words, after the earthquake the structure was shifted at the base, assuming an eccentric position. Also there are various fractures on the first section of the tower horizontally and diagonally crossing its perimeter walls, where a rigid motion on the order of centimetres was measured. The top of the structure collapsed at about 9 metres from the base toward the South-West side.

**Sensor installation and data processing.** The tower of San Giacomo Roncole is a slim structure with a shape characterized by several natural corners (see Fig. 1). Consequently, the measurements are performed without artificial corner reflectors installed on the body surface of the structure. This is an essential condition because the structure is seriously damaged. Dynamic surveys are carried out using three different configurations. In the first one, the IBIS-S system was placed in front of the tower in the South-East direction in order to monitor the dynamic behaviour of the full body of the structure with $30^\circ$ LOS angle. The second radar
The station was placed in the SW direction (30° LOS angle). The last acquisition was performed with the IBIS-S system located under the tower (70° LOS angle). The acquisition geometry was selected in order to reduce the effects of all possible noise sources, such as suspended cables and other metal structures, or trees and vegetation inside the radar profile. Each acquisition had a duration of about 10 min with a sampling frequency of 200 Hz. The vibrations of the building were monitored in real time during field operations. The Fourier spectra of signals were provided by processing the acquired data with IBIS Dataviewer and Matlab software in order to assess the main frequencies of the structure. Before of the spectral analysis, the displacement data were detrended and tapered with Hamming function to reduce leakage effects. The knowledge of the deformation kinematics allows to evaluate main vibration properties of the structure by means of the Frequency Domain Decomposition technique FDD (Brincker et al., 2001). This method is based on the Singular Values Decomposition of the output Power Spectral Density matrix \( \mathbf{G}_{yy} \) through the following Eq. (3):

\[
\mathbf{G}_{yy}(j\omega_i) = \mathbf{U}_i \mathbf{S}_i \mathbf{U}_i^H
\]

where \( \mathbf{U}_i \) is a unitary matrix of the singular vectors \( u_{ij} \), \( \mathbf{S} \) is a diagonal matrix of the scalar singular values \( s_{ij} \) and \( \mathbf{U}^H \) is the hermitian matrix of \( \mathbf{U} \) (complex conjugate transposed matrix). Assuming that each mode will be dominant around its corresponding frequency, the first singular vector represents an estimation of the mode shape and the corresponding singular value belongs to the auto-power spectral density function of the corresponding Single Degree Of Freedom system. By using this decomposition method, main modal parameters can be identified with high accuracy even in the case of strong noise contamination of the signals.

**Results and discussion.** The range-bins with high signal-to-noise ratio (SNR) along the radar power profile are associated with different natural back-scatterers located inside the radar scenario. However, the signal-to-noise ratio of the radar response from this structure is high and the structure is isolated inside the radar scenario. Thus several range-bins may be selected to be analyzed. Five range-bins of the radar power profile are selected to estimate fundamental vibration properties of the structure by means of the FDD decomposition technique. The radar-bins are selected in function of the distance along the radar line of sight between each radar-bin and the IBIS-S sensor. These range-bins correspond to five reflective points placed on the bell tower facade. This operation is easily performed knowing the geometric characteristics of the tower (the height of several architectonic elements such as windows and other ledges), the horizontal distance of the radar station, and the inclination of the IBIS-S head. The displacements retrieved from radar data are shown in Fig. 2. These time series have been obtained observing the tower from a position to the base of the tower, at a distance of 23 metres.
During all measurements a regular wind with moderate speed of 5.5 m/s blew.

The displacement spectra are obtained over the whole recorded ten minutes signal. A band-pass filter (0.3Hz-10Hz) was applied to reduce the presence of disturbances linked to atmospheric effects and to vibration of the sensor itself. The influence of the first effect is prevalent on the measured phases and, as a consequence, on the estimated displacements with long period (0.1-0.2Hz). Another effect is caused by the vibration of the measurement tool. Luzi et al. (2012) observe that the measured resonant frequency of the system ranges within

Fig. 2 – One minute record acquired with the second configuration: LOS displacement retrieved from radar data as a function of the time. The time histories refer to two range-bins selected from the radar power profile and correspond to different heights of the tower.

Fig. 3 – a) Sinusoidal trend of the displacement record obtained for the 50th range-bin (30 metres height). b) Frequency analysis of the same time-history.
10 Hz±2 Hz for typical working conditions. Then a low-pass filtering may be applied in order to assure that the measured vibrations are not imputable to the natural response of the tripod-head sensor system. All amplitude spectra are characterized by a clear harmonic component at 0.96 Hz (corresponding period of 1.04 s) whose amplitude increases with the height of the analyzed range-bin. This behaviour agrees with the expected amplitude variation associated at the first natural mode (simple bending). This periodicity cannot be directly retrieved from all displacement time series but only for the 50th range-bin corresponding to the reflection from the height of 30 metres on the tower (see Fig. 3).

The obtained value of 0.96 Hz could be influenced by the presence of structural damage caused by the earthquake. This value could be compared with the theoretical one achieved through numerical modelling of the building before the damage. However, even without a direct model, several empirical relationships available for masonry structures, like those proposed by the Italian Building Code NTC-2008, the Spanish National Code NSCE-02 and by literature studies (Rainieri and Fabbrocino, 2012), are used to assess the fundamental frequency of vibration. The obtained results range between 1.4 and 1.5 Hz. The significant difference (31-36%) between the experimental value and the estimated values could be imputed to the damage caused by the earthquake. It is generally recognised that the period of vibration grows while increasing the mass of the vibrating system and while reducing the stiffness.

The radar measurements allows the evaluation of the dynamic behaviour (amplitude of vibration) of several parts of the building located at different heights. In this case we have monitored the structure from different perspectives and we have compared the experimental mode shapes obtained for the IBIS-S configurations 1 and 2. The mode shape retrieved by the configuration 3 was not used for this analysis because the displacements measured in LOS direction are not comparable with the others. In fact, in this configuration the microwave sensor is more inclined (70°) and is placed at short distance from the tower (8 metres). Measured displacements along two directions are projected along the horizontal plane. The experimental mode shapes show a similar trend. We observe that maximum values are measured from St 02 IBIS-S station and are characterized by amplitude ranges from 0.05 to 0.2 mm. The fundamental mode of vibration is a bending mode with the same frequency of 0.96 Hz in both directions of measurement. Anomalous behaviour is detected at the point placed at 17 metres height with experimental measured displacements greater than those expected. This trend could be correlated with the structural damages of the building at the middle level. Moreover, the larger displacements obtained in the second acquisition are justified by the major shift recorded in this direction (about 2 cm) due to seismic action.

Conclusions. This paper proposes the use of the ground-based microwave interferometry for remote sensing of vibrations of structures aimed at providing useful information for specialists about the damage state of structures in areas affected by earthquakes. For this reason, this work is the first application of ground-based radar interferometry to the study of an inaccessible damaged building. The authors report the results of the experimental dynamic test aimed at estimating the vibrations of an historical bell tower in an urban environment, performed through ambient vibration testing. Also, the basic principle of the interferometric technique has been briefly resumed and the main experimental data obtained for the vibration features of the structure have been critically discussed to identify anomalous dynamic behaviours linked to structural damages. In general, the proposed method can estimate displacements ranging from a few microns up to several millimetres for large structures, ranging from thin and tall structures to other types of buildings (towers, skyscrapers and bridges). The possibility of working remotely makes this approach suitable for the dynamic control of buildings that have reported structural damage after an earthquake, especially for civil structures of strategic interest during the emergency and for cultural heritage buildings which represent the history and the social identity of a community.

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